

# Anisotropic scattering in rotational collisions of electrons with CO molecules

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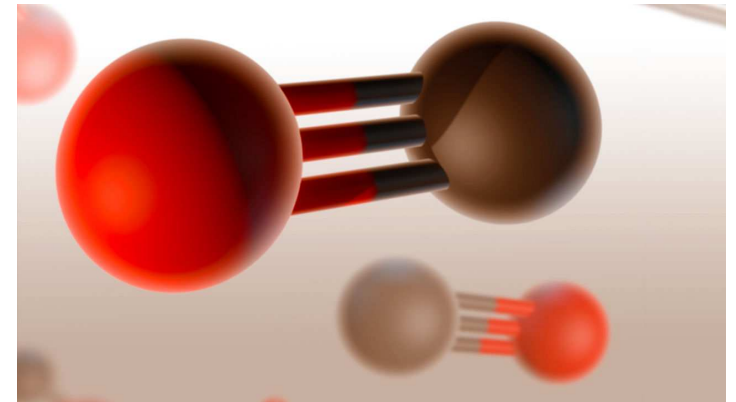
<https://www.ipfn.tecnico.ulisboa.pt/nprime/>

# Anisotropic e-CO rotational collisions

## Why CO ?

### Planetology

- Earth, Mars, Jupiter (Cameron bands  $a^3\Pi \rightarrow X^1\Sigma$ )
- re-entry Physics



### Astrophysics

- second most abundant gas in molecular clouds, after hydrogen (rotational excitation of CO by photoelectrons and subsequent emission of radiation)

### Plasma applications

- reforming of CO<sub>2</sub>
- deposition: CO adsorption on surfaces

## Why e-CO rotational collisions ?

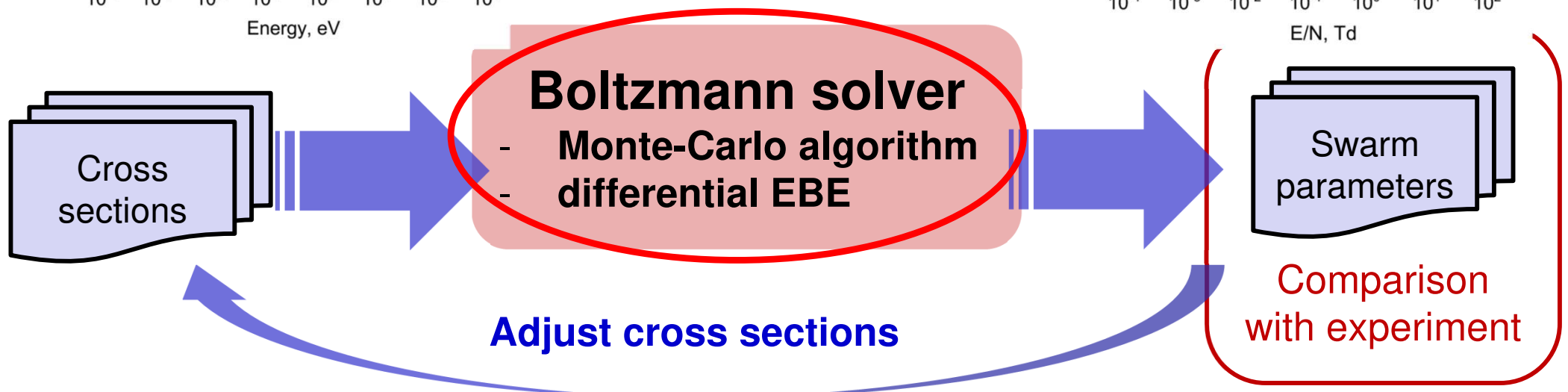
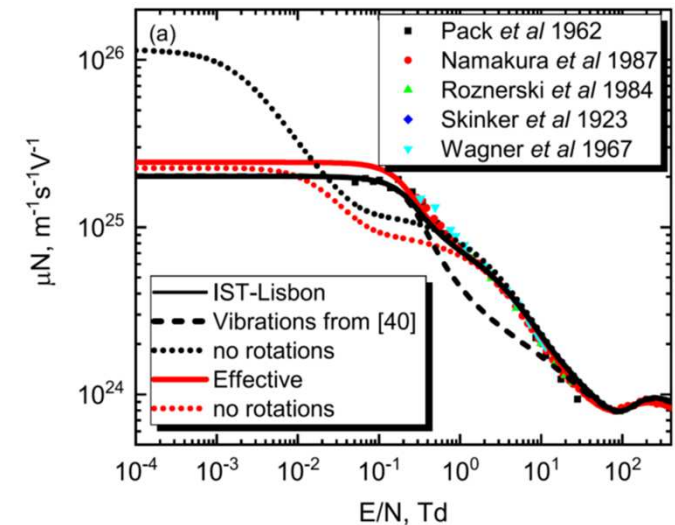
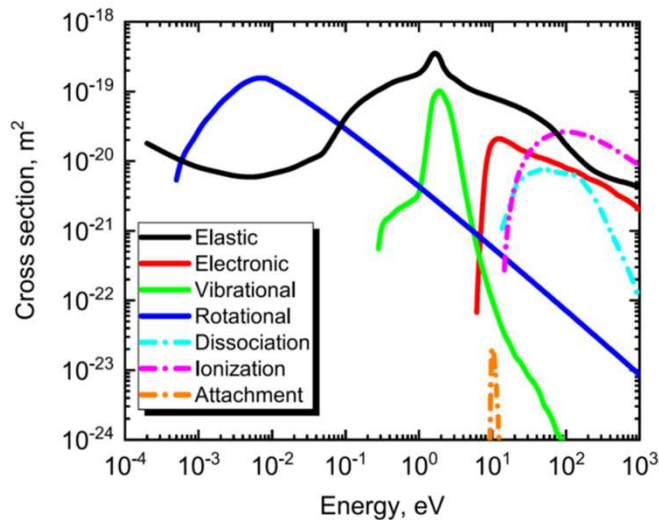
Reviews of electron-collision cross sections (CS) and swarm parameters

- Comprehensive reviews (no complete CS sets)
  - Trajmar et al, *Phys. Rep.* 97 (1983)
  - Brunger and Buckman, *Phys. Rep.* 357 (2002)
  - Raju, *Gaseous electronics: theory and practice*, CRC Press (2005)
  - Y. Itikawa, *J. Phys. Chem. Ref. Data* 44 (2015)
- Complete swarm-derived CS sets (**Phelps database on LXCat**)
  - Hake and Phelps, *Phys. Rev.* 158 (1967)
  - Land, *J. Appl. Phys.* 49 (1978)
  - use of total momentum-transfer CS determined as the sum of a dipole term, calculated as a dipole rotational with the Born approximation and a nitrogen-like elastic CS
- Recent complete swarm-derived CS set (**IST-Lisbon database on LXCat**)
  - P. Ogloblina et al, *PSST* (2020)
  - analysis of CS at low energies (predominance of electron-dipole rotational interactions)
  - proposal of elastic momentum-transfer CS obtained from an adjusted effective (total)

**Two-term approximation calculations**

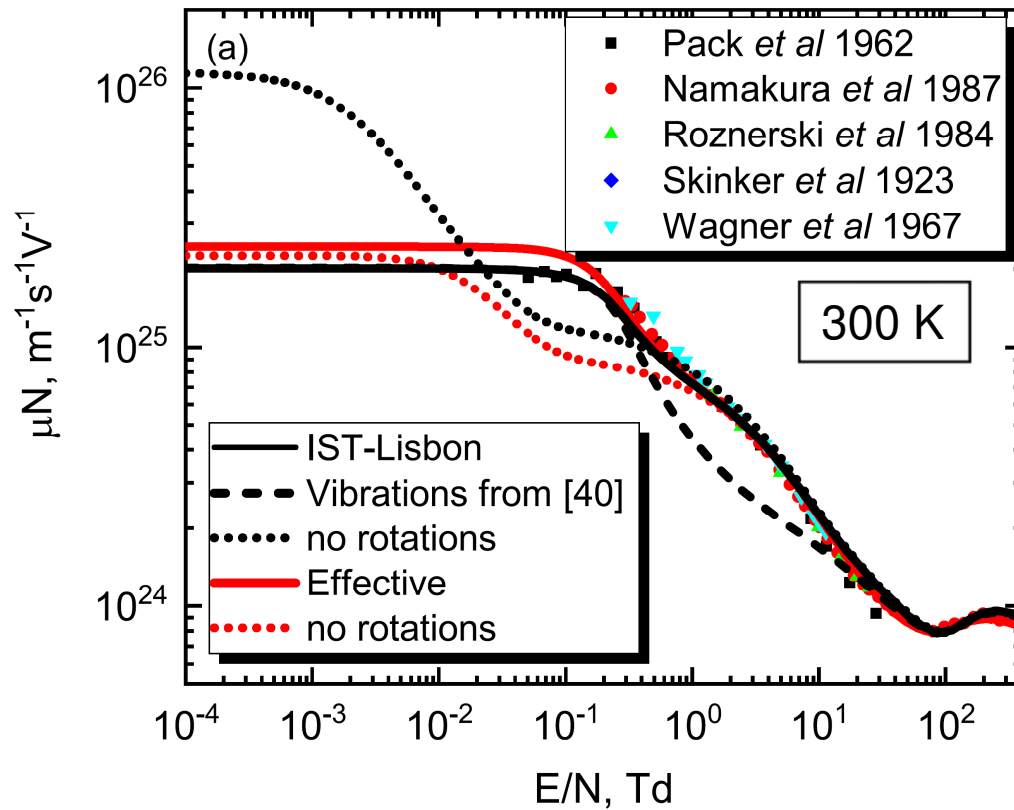
# Swarm-derivation of complete sets of cross sections

**Complete sets of cross sections** are those describing the total transfer of momentum and energy between electrons and the gas

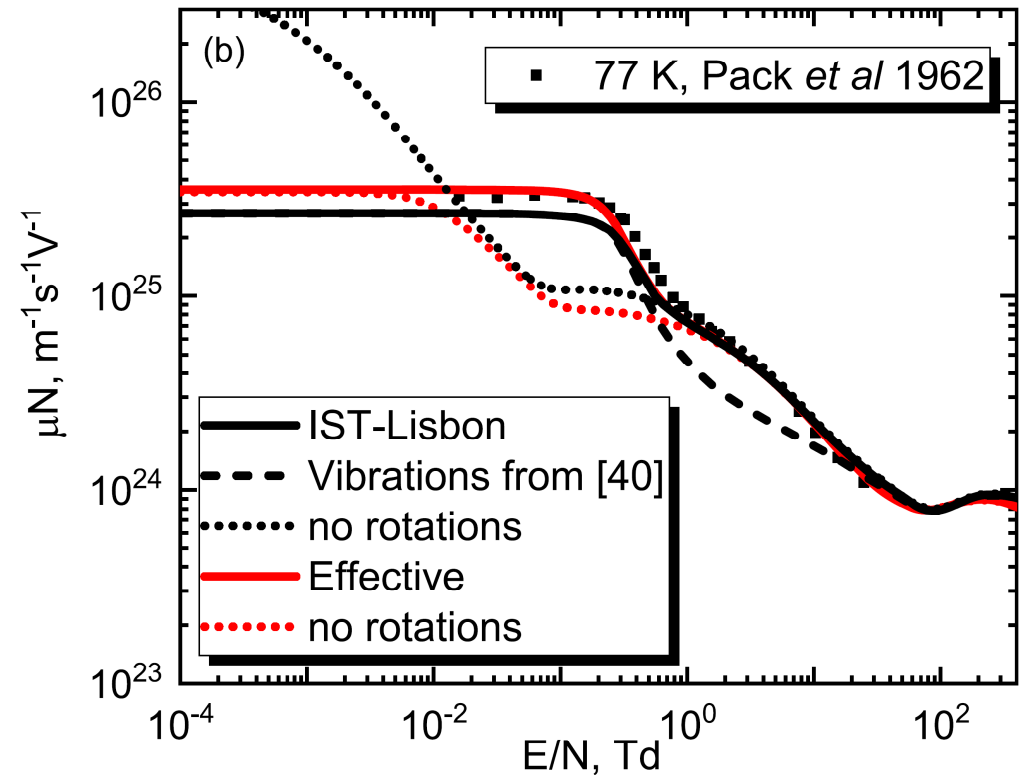


# Anisotropic e-CO rotational collisions

## Why e-CO rotational collisions ?



P. Ogloblina et al, *PSST* 29 (2020)



< 20% disagreement !

There is room for improving swarm predictions

# Anisotropic e-CO rotational collisions

## Why anisotropic effects ?

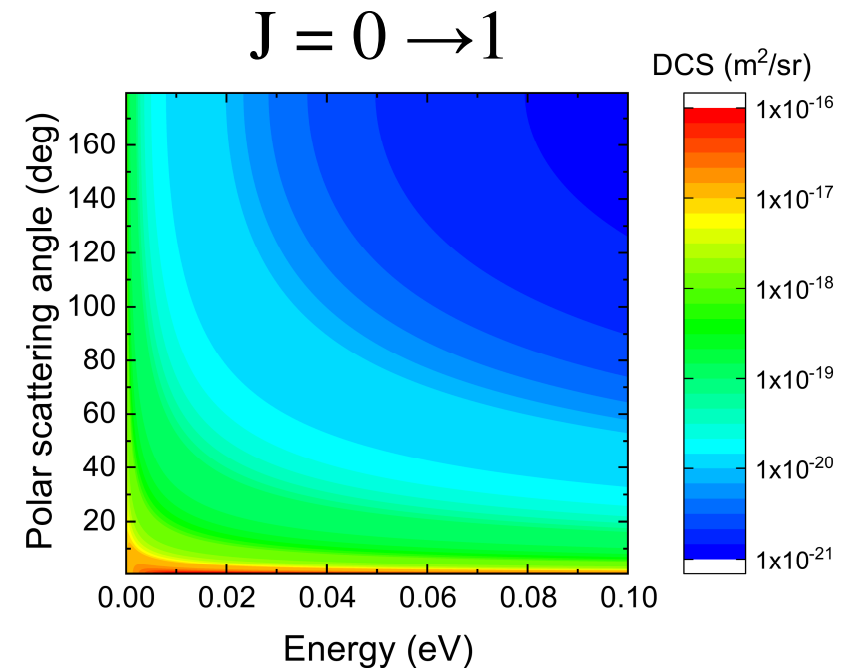
The differential cross section (DCS) for polar molecule CO  
(Born approximation combined with point dipole interaction, for low energy region)

Y. Itikawa, *J. Phys. Chem. Ref. Data* 44 (2015)

$$\frac{d\sigma(\epsilon, \theta)}{d\Omega} = \frac{4(a_0\mu)^2 R_\infty}{3K^2} \sqrt{\frac{\epsilon'}{\epsilon}} \frac{J_{>}}{2J+1}$$

$$K^2 = |\mathbf{k}' - \mathbf{k}|^2 = \epsilon' + \epsilon - 2\sqrt{\epsilon\epsilon'} \cos\theta$$

$$J_{>} = \max(J, J')$$



**The scattering distribution is highly anisotropic**

## Anisotropic e-CO rotational collisions

L Vialletto et al, *PSST* 30 075001 (2021)

- **The e-CO cross sections**

Integral and momentum-transfer cross sections for rotational collisions  
Complete sets of cross sections adopted; swarm derivation

- **Swarm calculations and results**

MC code (+ angular scattering model)  
The two-term LibOn Kinetics Boltzmann solver (LoKI-B)  
Swarm results

- **Improving the two-term solver LoKI-B**

Implementation of anisotropic rotational cross sections  
Swarm results

- **Final remarks**

Apologies for some busy slides

# The e-CO rotational cross sections

## Integral cross section and momentum-transfer cross section

### The integral cross section (ICS)

$$\sigma_{J,J+1}^{ICS}(\epsilon) = 2\pi \int_0^\pi \frac{d\sigma(\epsilon, \theta)}{d\Omega} \sin\theta d\theta = \frac{(a_0\mu)^2 R_\infty}{V_{J,J+1}} \frac{J+1}{2J+1} f(\epsilon/V_{J,J+1})$$

### The momentum-transfer cross section (MT)

T. Makabe and R. White, *JPD* 48 (2015)

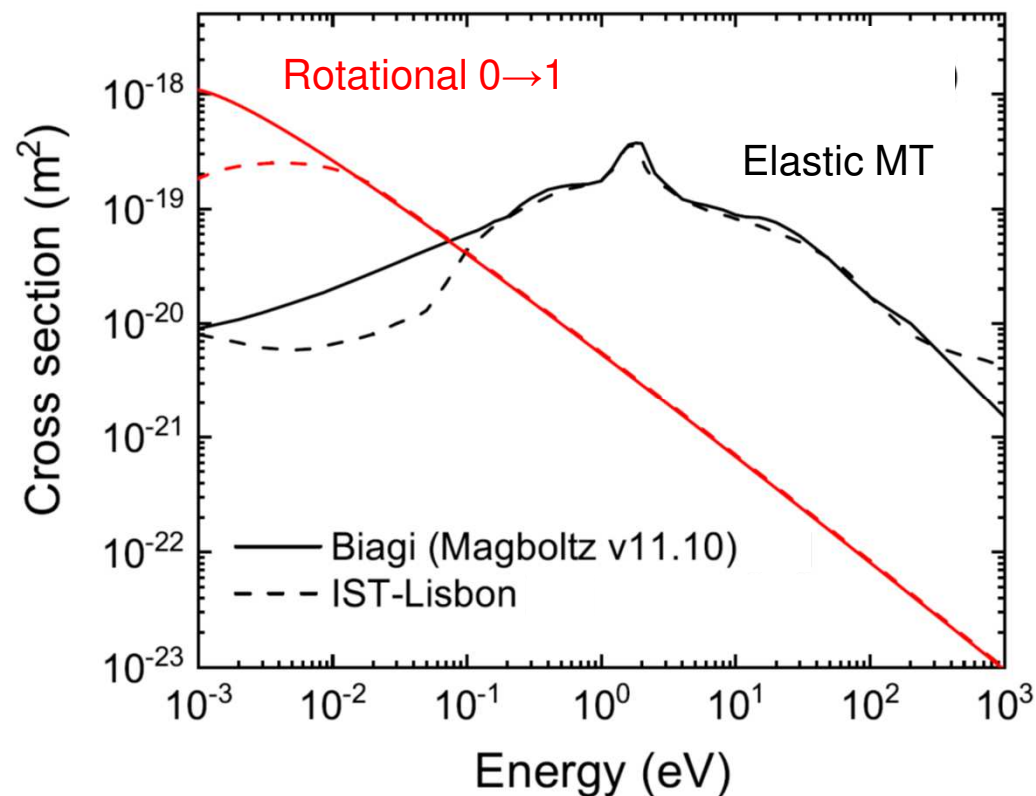
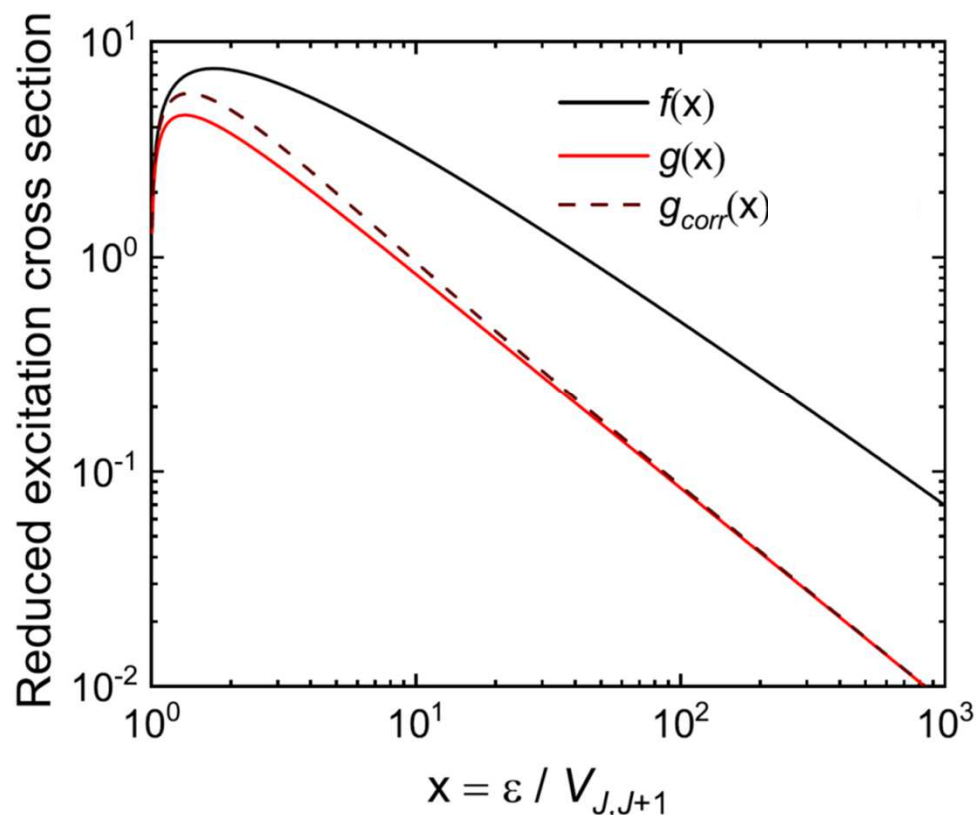
$$\sigma_{J,J+1}^{MT}(\epsilon) = 2\pi \int_0^\pi \frac{d\sigma(\epsilon, \theta)}{d\Omega} \left[ 1 - \left( 1 - \frac{V_{J,J+1}}{\epsilon} \right)^{1/2} \cos\theta \right] \sin\theta d\theta.$$
$$= \frac{(a_0\mu)^2 R_\infty}{V_{J,J+1}} \frac{J+1}{2J+1} g_{corr}(\epsilon/V_{J,J+1})$$

$g(\epsilon/V_{J,J+1})$



# The e-CO rotational cross sections

ICS and MT: swarm-derivation of IST-Lisbon cross sections



## Swarm-derivation of IST-Lisbon CS

Too small

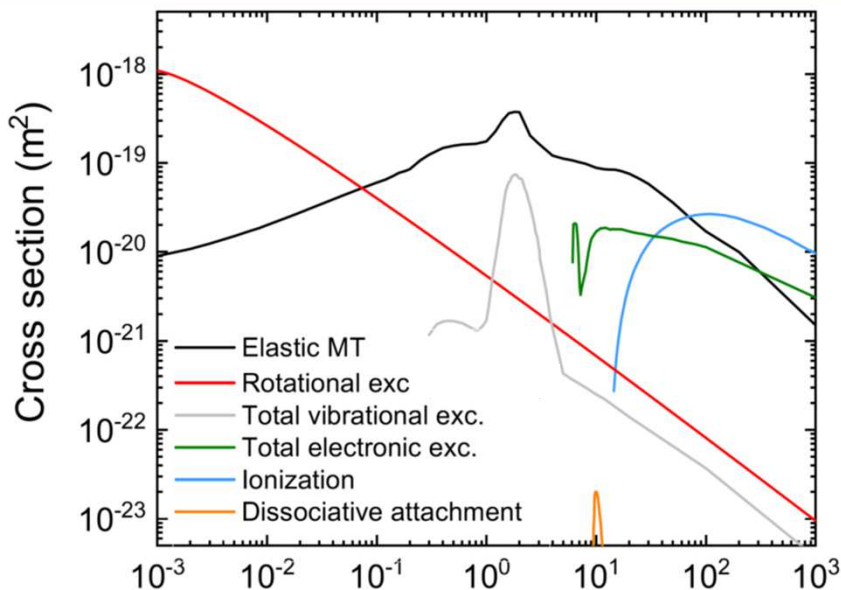
$$\sigma_{\text{elastic-MT}} = \sigma_{\text{effective}} - \sum_J \sigma_{J,J+1}^{MT}$$

Assuming isotropy

Too large: adjust / reduce

# The e-CO cross sections

Complete sets of cross sections adopted

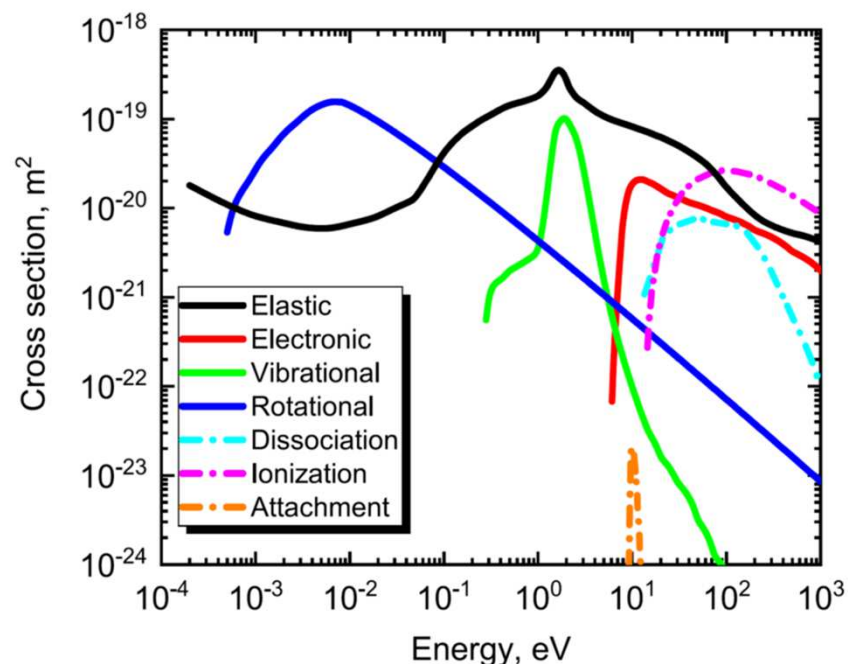


## Biagi's Magboltz v11.10

<http://magboltz.web.cern.ch/magboltz/>

Vibrational excitations / deexcitations involving  $v=0-6$   
agree with Laporta et al, *PSST 21* (2012), divided by 1.3  
Electronic excitations (including diss attach & ionization)  
mostly Sawada et al, *J. Geophys. Res 77* (1972)

Rotational excitations / deexcitations involving  $J=0-26$   
with ICS from dipole-Born DCS  
but adopting a different angular scattering model



## IST-Lisbon

P. Ogloblina et al, *PSST 29* (2020)

Vibrational excitations / deexcitations involving  $v=0-10$   
Laporta et al, *PSST 21* (2012)  
Electronic excitations (including diss attach & ionization)  
Sawada et al, *J. Geophys. Res 77* (1972)  
Itikawa, *J. Phys. Chem. Ref. Data 44* (2015)

Rotational excitations / deexcitations involving  $J=0-16$   
adjusted ICS

# Swarm calculations

## Monte Carlo code

L. Vialetto et al, *PSST* 29 (2020)

- adopts null-collision method
- adopts a modified time-step technique
- includes the effects of the finite temperature of the background gas, with an exact Test Particle Monte Carlo technique
- describes e-neutral scattering events in the centre-of-mass frame
- uses a standard Time-Of-Flight method to calculate bulk transport parameters
- follows the trajectories of typically  $\sim 10^4 - 10^5$  electrons
- defines the steady-state time  $t_{SS}$ , for a deviation of the mean kinetic energy  $< 0.1\%$
- improves statistics by averaging the bulk transport parameters in the interval  $[t_{SS}, 10 t_{SS}]$  with a sample time of  $10^{-9}$  s

# Swarm calculations

## Monte Carlo code - angular scattering model

### Angular distribution function

$$I(\epsilon, \theta) = \frac{1}{\sigma^{ICS}(\epsilon)} \frac{d\sigma(\epsilon, \theta)}{d\Omega}$$

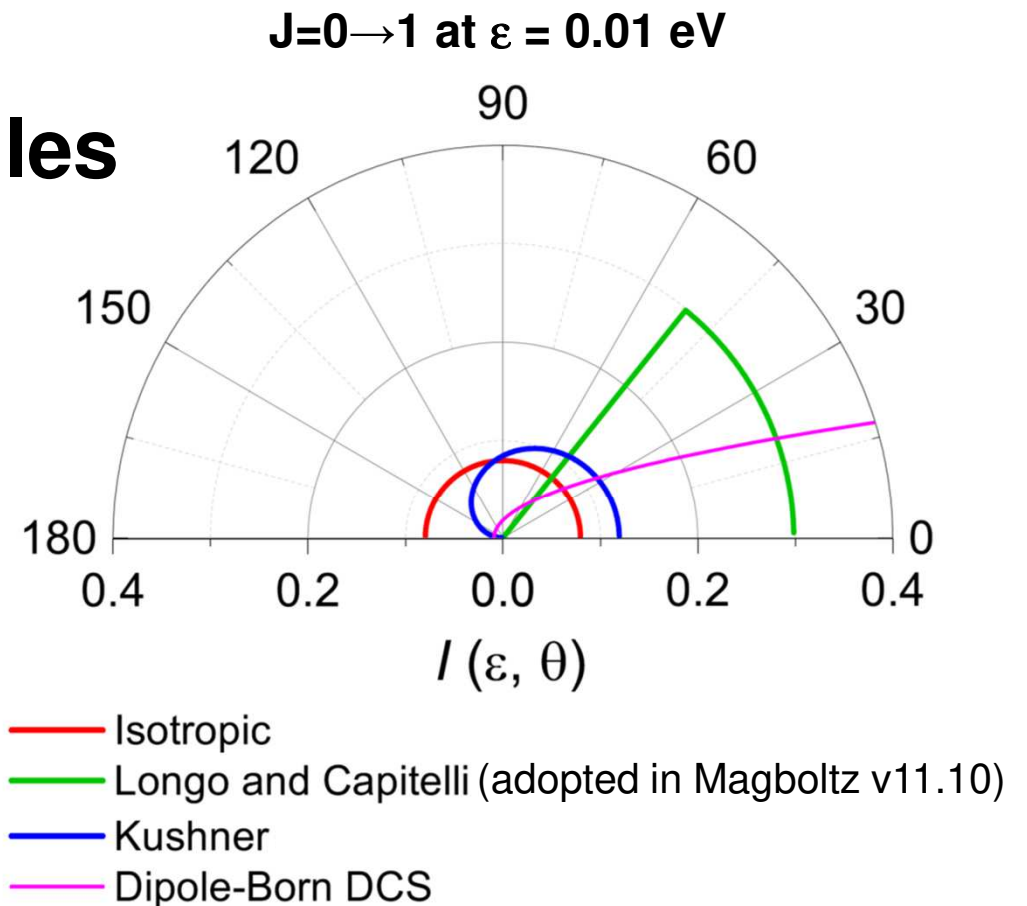
### Sampling of scattering angles

$$r_i = 2\pi \int_0^{\theta_i} I(\epsilon, \theta') \sin \theta' d\theta'$$

### Dipole-Born DCS

$$\cos \theta_i = 1 + \frac{2\xi^2}{1 - \xi^2} (1 - \xi^{-2r_i})$$

$$\xi(\epsilon) = \frac{V_{J,J\pm 1}}{(\sqrt{\epsilon \pm V_{J,J\pm 1}} + \sqrt{\epsilon})^2}$$



# The LisbOn Kinetics Boltzmann solver (LoKI-B)

(developed under MATLAB®)

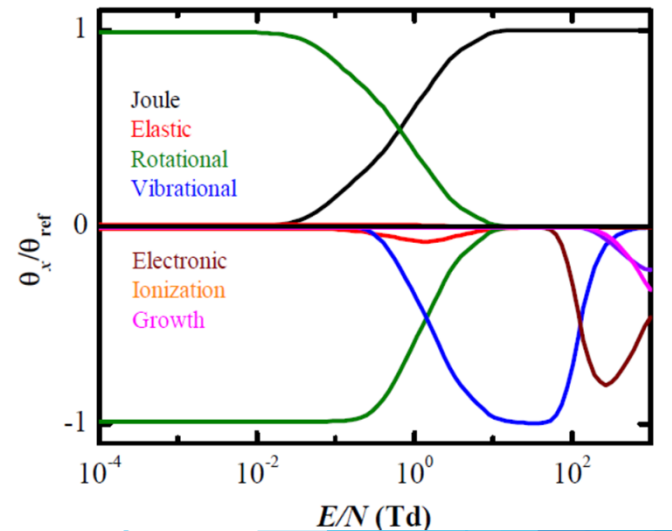
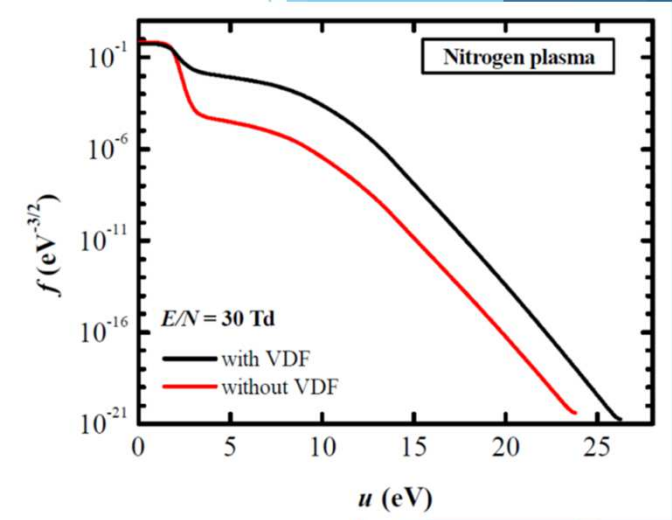


**OPEN SOURCE**

## LoKI-B

<https://github.com/IST-Lisbon/LoKI>

- solves the time and space independent form, or the time-dependent form, of the two-term electron Boltzmann equation
- includes e-e collisions, CAR operator, and growth models for the electron density.



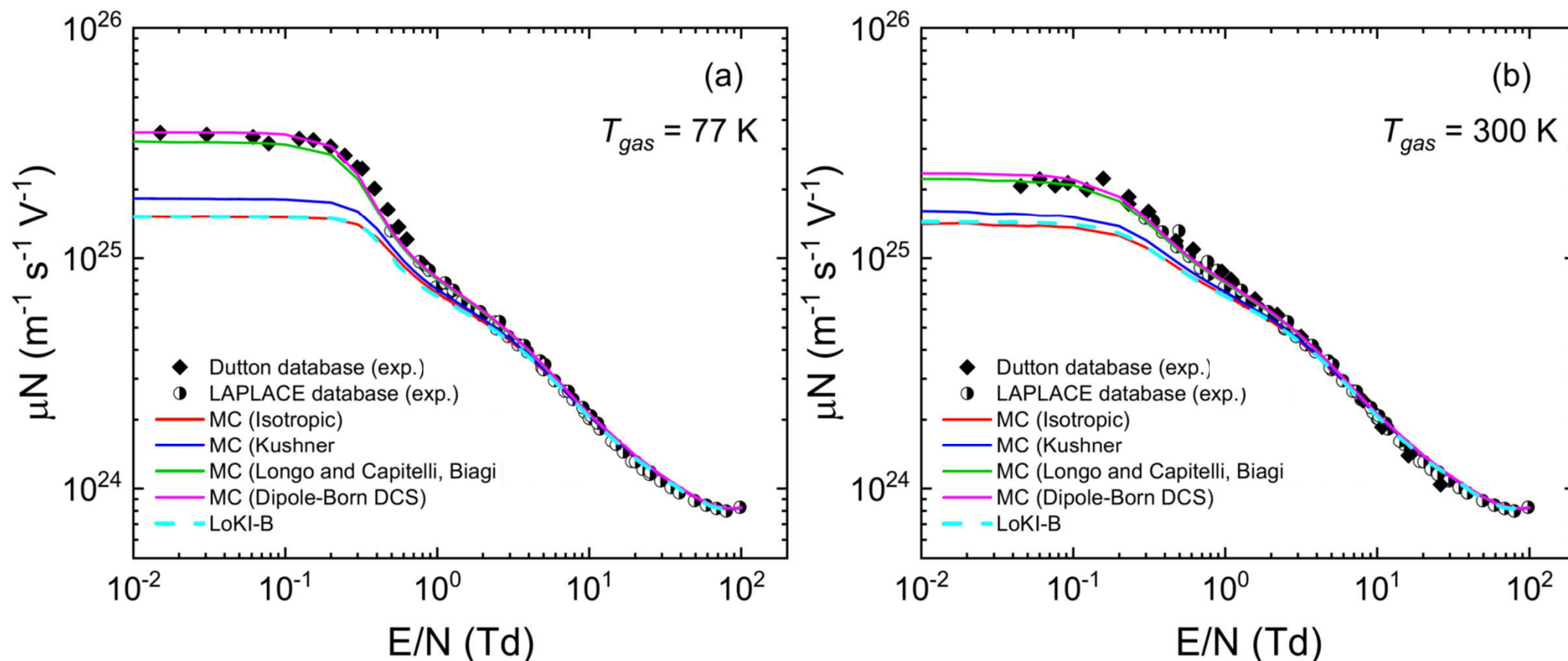
## The LisbOn Kinetics Boltzmann solver

was developed as a response to the need of having an electron Boltzmann solver easily addressing the **simulation of the electron kinetics in any complex gas mixture** (of atomic / molecular species), describing first and second-kind electron collisions with **any target state** (electronic, vibrational and rotational), characterized by **any user-prescribed population**.

A. Tejero-del-Caz *et al* Plasma Sources Sci. Technol. 30 (2021) 065008

# Swarm results - I

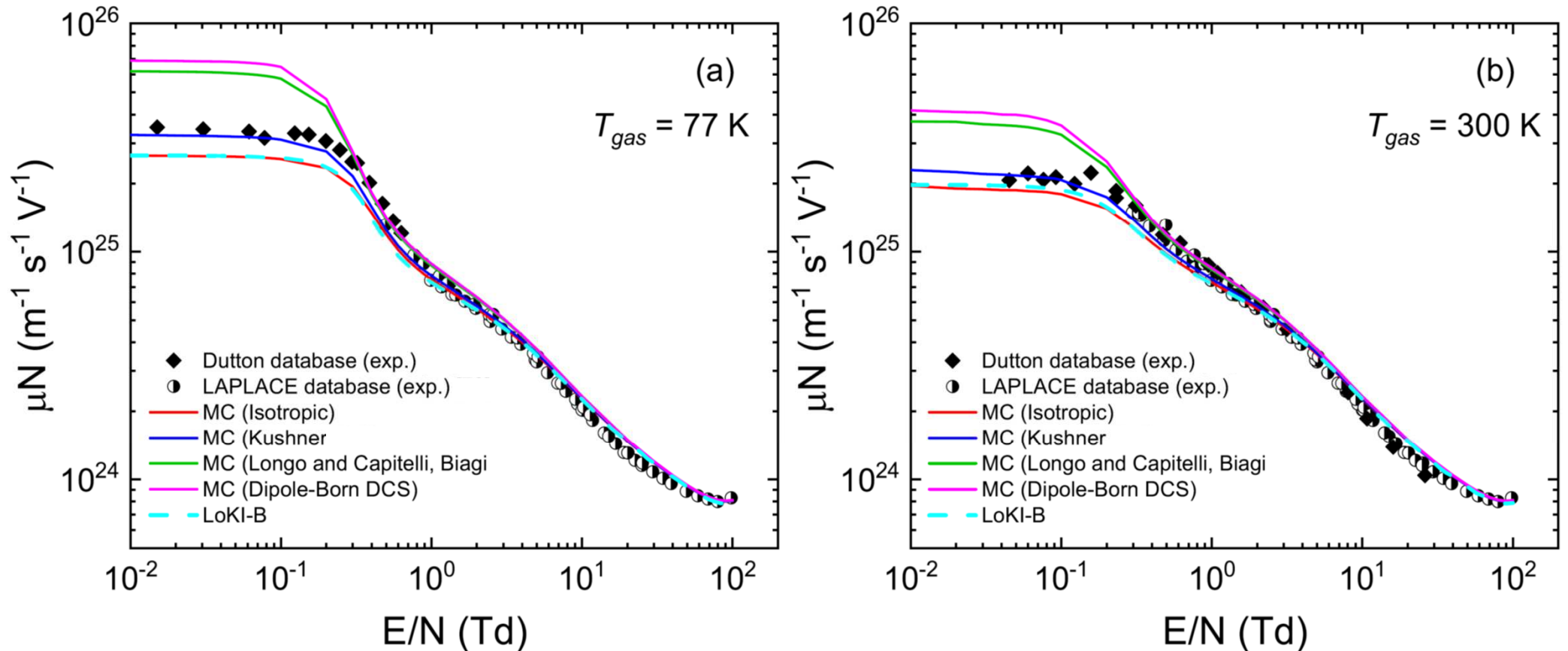
## Biagi cross sections



- Excellent agreement between MC (isotropic) and LoKI-B
- 2% agreement between MC (dipole-Born DCS) and experiment
  - at 300 K
  - at 77 K for  $E/N < 0.2 \text{ Td}$ ,  $E/N > 0.8 \text{ Td}$  (8% in other cases)

# Swarm results - II

## IST-Lisbon cross sections



- Between MC (isotropic) / LoKI-B and experiment
  - agreement below 1% at 300 K
  - up to 20% disagreement at 77 K
- Between MC (dipole-Born DCS) and experiment
  - disagreement between 30% (300 K) and 50% (77 K), for this cross section set

# Improving the two-term solver LoKI-B

## Implementation of anisotropic rotational CS

### Expanding the DCS in Legendre polynomials

Makabe and Petrovic, *Plasma electronics: applications in microelectronic device fabrication* (2014)

$$\frac{d\sigma_k(\epsilon, \theta)}{d\Omega} = \sum_{j=0}^{\infty} \frac{2j+1}{4\pi} \sigma_k^j(\epsilon) P_j(\cos \theta)$$

$$\sigma_k^j(\epsilon) = 2\pi \int_0^{\pi} \frac{d\sigma_k(\epsilon, \theta)}{d\Omega} P_j(\cos \theta) \sin \theta d\theta \quad \dots \text{orthogonality relation}$$

By truncating the expansion to the first order

$$\sigma_{J,J+1}^{ICS}(\epsilon) \simeq \sigma_{J,J+1}^0(\epsilon)$$

$$\sigma_{J,J+1}^{MT}(\epsilon) \simeq \sigma_{J,J+1}^0(\epsilon) - \sigma_{J,J+1}^1(\epsilon)$$

**The angular distribution of scattering can be described using only ICS and MT cross sections**



### The updated first anisotropy equation

$$f_1(\epsilon) = -\frac{E}{N} \frac{1}{\Omega_c(\epsilon)} \frac{df_0(\epsilon)}{d\epsilon}$$

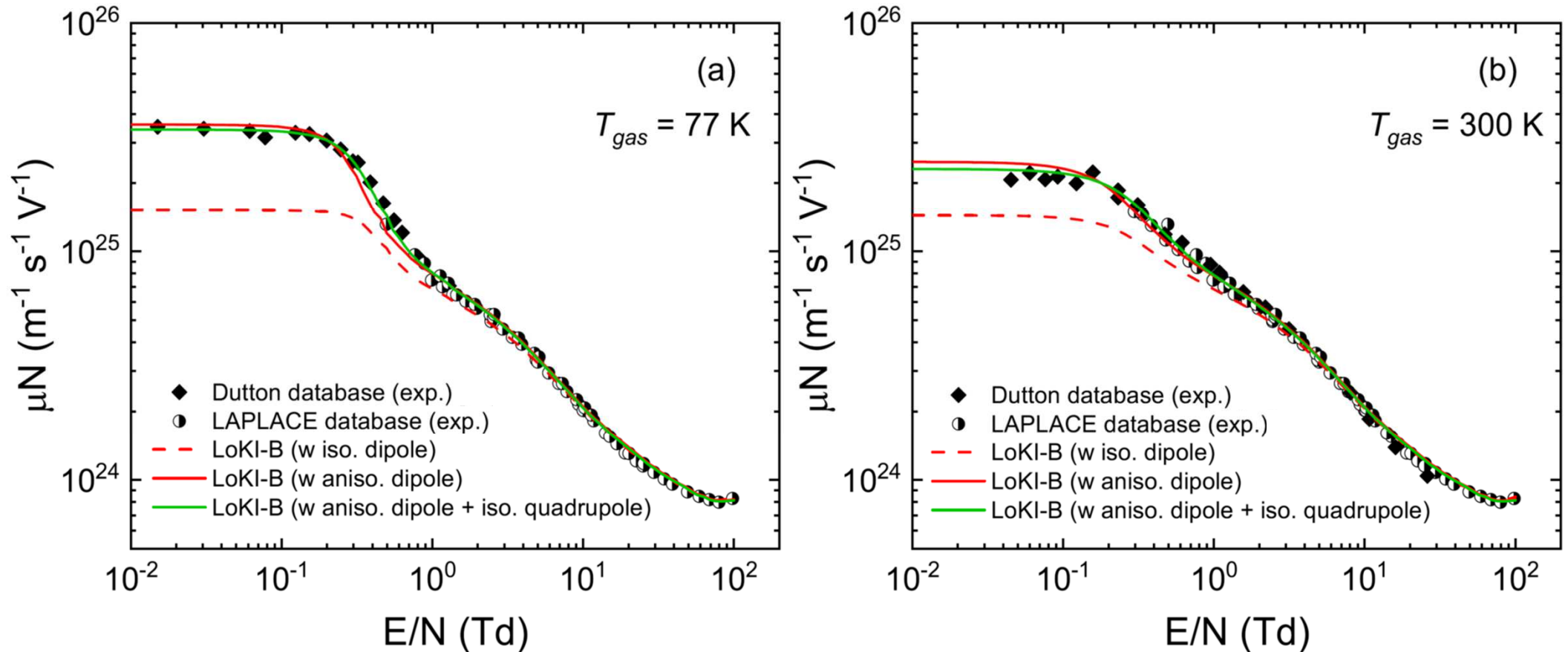
$$\Omega_c(\epsilon) \simeq \sum_i \delta_i \sigma_{i,ela}^{MT}(\epsilon) + \sum_{i,j>i} \left[ \delta_i \sigma_{i,j}^0(\epsilon) + \delta_j \frac{g_i \epsilon + V_{i,j}}{g_j \epsilon} \sigma_{i,j}^0(\epsilon + V_{i,j}) \right]$$

$$+ \sum_{J,J+1} \left[ \delta_J \sigma_{J,J+1}^{MT}(\epsilon) + \delta_{J+1} \frac{g_J}{g_{J+1}} \sigma_{J,J+1}^{MT}(\epsilon) \right] \dots \text{for negligible } V_{J,J+1} \text{ energies}$$

The improved treatment distinguishes between ICS and MT cross sections for rotational collisions

# Swarm results - III

## Improved LoKI-B with Biagi cross sections



Between improved LoKI-B and experiment

- agreement within 8% (at intermediate  $E/N$  values) with anisotropic dipole rotational collisions
- excellent agreement (below 2%) with anisotropic dipole rotational collisions + isotropic quadrupole rotational collisions

# Final remarks

- **Investigation of the e-CO anisotropic scattering in rotational collisions**
  - swarm calculations and comparison with measurements
  - MC code and two-term Boltzmann solver (LoKI-B)
  - adopting Biagi's complete set of cross sections (Magboltz code v11.10) combined with ICS coherently deduced from dipole-Born DCS for rotations
- **Use of dipole-Born DCS for rotational collisions in CO**
  - allows proposing a novel forward-peaked model for MC simulations
  - enables implementing anisotropic dipole rotational collisions, in two-term solvers
  - leads to good agreement (within few percent) between simulations (MC and two-term) and measurements of swarm parameters in CO
    - (improved agreement after including isotropic quadrupole rotational collisions)
- **Use accurate DCS in future research on electron swarms**
  - the calculation of swarm parameters is more influenced by the choice of the angular scattering model (deviations up to 50%) than the adoption of the two-term approximation
  - Extend the study to other collisional mechanisms (e.g. vibrations), even in two-term solvers (with partial cross sections derived from Legendre polynomials expansion of DCS)

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# FCT

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